

AMERICAN UNIVERSITY OF BEIRUT
CIVE 210 STATICS

EXAM I: 8:00 – 9:30 AM
Spring 2007-2008
Student Name:

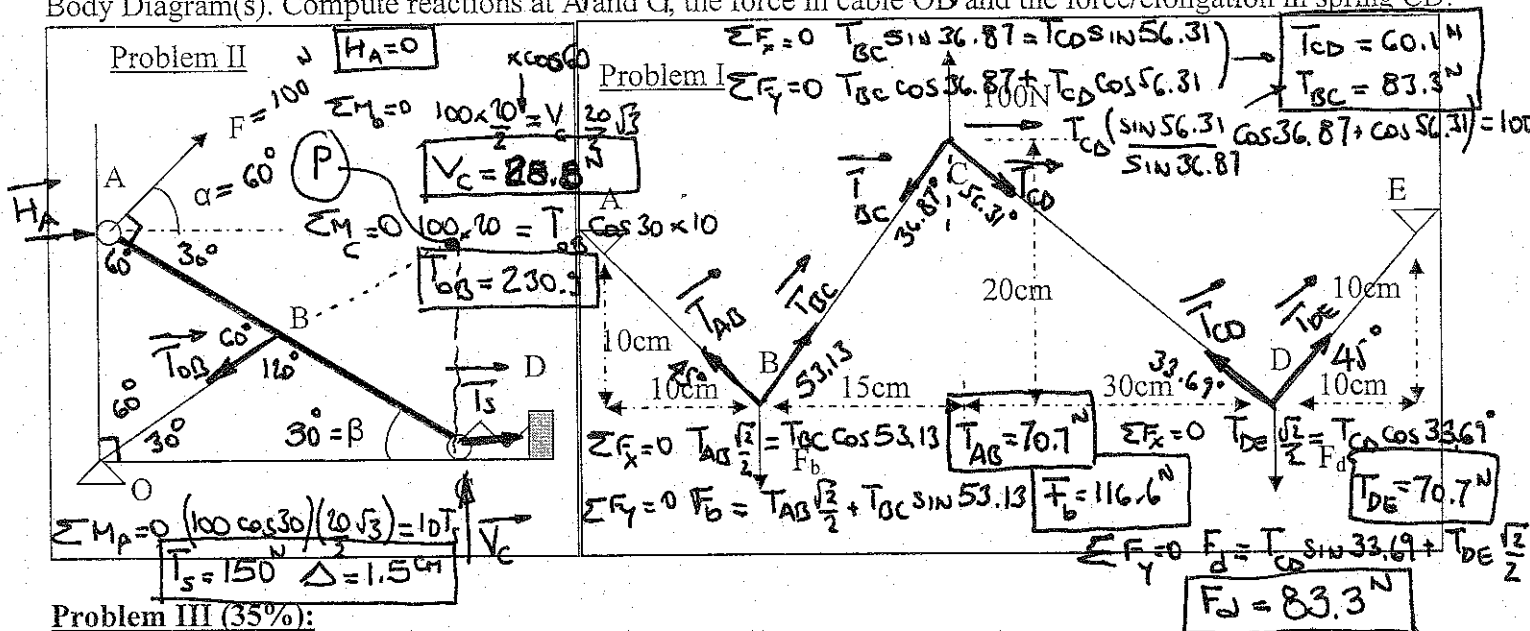
Mar 29, 2008
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Student ID:

Problem I (30%):

A single weightless piecewise cable ABCDE is hinge supported at A and E as shown. The cable is loaded with vertical concentrated forces F_b (down) at B, 100N (up) at C and F_d (down) at D as shown. Assuming geometry as shown, draw Free Body Diagram(s), and compute the tension forces in cable segments AB, BC, CD and DE as well as the applied forces F_b and F_d required for equilibrium.

Problem II (35%):

A rigid, homogeneous, weightless and uniform bar ABC is roller supported at A against a vertical wall, roller supported at C against a horizontal surface, connected to a rigid weightless cable OB and to a spring CD of spring stiffness $K=100\text{N/cm}$. Assume a 100N force F is applied at point A oriented at an angle α to the horizontal direction. Assume roller support at A is barely touching the vertical wall, cable OB is hinged at O, frictionless and dimensionless roller supports, $\alpha = 60^\circ$ and $\beta = 30^\circ$. Assume $AB = BC = OB = 10\text{cm}$, draw Free Body Diagram(s). Compute reactions at A and C, the force in cable OB and the force/elongation in spring CD.



Problem III (35%):

For the three dimensional system shown, draw Free Body Diagram(s) and compute the tension forces in cables AB and AC as well as the compression force in bar AO. Assume F is a vertical force of magnitude 150N. Assume weightless system. Use Cartesian Formulation.

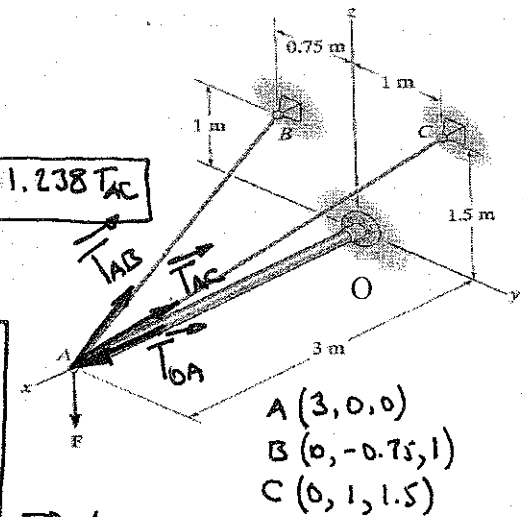
$$\sum \vec{F} = 0 \quad \vec{T}_{AB} + \vec{T}_{AC} + \vec{T}_{AO} + \vec{F} = 0$$

$$(1) \quad T_{AB} \frac{3}{3.25} + T_{AC} \frac{3}{3.5} + T_{AO}(+1) = 0 \quad \leftarrow \sum F_x = 0$$

$$(2) \quad T_{AO} \frac{-0.75}{3.25} + T_{AC} \frac{1}{3.5} + 0 = 0 \quad \leftarrow \sum F_y = 0 \quad \Rightarrow T_{AO} = 1.238 T_{AC}$$

$$(3) \quad T_{AB} \frac{1}{3.25} + T_{AC} \frac{1.5}{3.5} + 0 - 150 = 0 \quad \leftarrow \sum F_z = 0$$

$$\begin{aligned} (3) + (2) &\rightarrow T_{AC} = 185.3\text{N} \\ (2) &\rightarrow T_{AB} = 229.4\text{N} \\ (1) &\rightarrow T_{AO} = 370.6\text{N} \end{aligned}$$



$$\vec{AB} = (-3, -0.75, 1) \quad \vec{AC} = (-3, 1, 1.5) \quad \vec{AO} = (-3, 0, 0)$$

$$\vec{u}_{AB} = \frac{-3}{3.25}\vec{i} - \frac{0.75}{3.25}\vec{j} + \frac{1}{3.25}\vec{k}$$

$$\vec{u}_{AC} = \frac{-3}{3.5}\vec{i} + \frac{1}{3.5}\vec{j} + \frac{1.5}{3.5}\vec{k}$$

$$\vec{u}_{AO} = -\vec{i}$$